

大葉大學九十三年學年度轉學招生考試試題紙

系 組 別	日\ 第二部	年級	考 試 科 目 (中文名稱)	考試日期	節次	備註
資訊管理系	日間	二	微積分	7月19日	三	共一頁

註：考生可否攜帶計算機或其他資料作答，請在備註欄註明（如未註明，一律不准攜帶）

11:10 ~ 12:30

Part I. 填充題(只需寫出答案即可，但請務必標明題號；每個空格 5 分，共 30 分)

1. Evaluate $\lim_{x \rightarrow 4} \frac{\sqrt{x} - 2}{x - 4} =$ _____

2. Find the derivative of $f(x) = 4x^3 \cdot \ln x$. _____

3. Use logarithmic differentiation to find the derivative of $f(x) = x^{\sin x}$. _____

4. Evaluate $\int \frac{1+e^x}{e^x} dx =$ _____

5. Evaluate $\int 2t\sqrt{t^2 - 1} dt =$ _____

6. Evaluate $\int \left(\frac{1}{x^2} - \frac{3}{x^3} \right) dx =$ _____

Part II. 計算題(請詳列計算過程，否則不予給分；此部分共 70 分)

1. Using implicit differentiation to determine $\frac{dy}{dx}$ for $5x^3 + y^3 - x^4 = 0$ (10%)

2. Let $y = \frac{x+2}{x-1}$ at $x = 2$, Find an equation of the tangent line (10%)

3. Obtain the following questions on the graph of $f(x) = x + \frac{1}{x}$: (30%)

1. Find the horizontal and vertical asymptotes of $f(x)$

2. Find the critical point(s) of $f(x)$

3. Determine the intervals where $f(x)$ is increasing and where $f(x)$ is decreasing

4. Determine the intervals where $f(x)$ is concave upward and where $f(x)$ is concave downward

5. Find the inflection point(s) of $f(x)$

6. Sketch the graph of $f(x)$

4. Determine $\int (x+3)e^x dx$ (10%)

5. Determine the area bounded by the given curves. $f(x) = 3x^2 - 2x$ and $g(x) = x^3$. (10%)