

大葉大學九十二學年度轉學招生考試試題紙

系 組 別	日 \ 第二部	年級	考 試 科 目 ( 中 文 名 稱 )	考試日期	節次	備註
資訊管理系	日間	二	微積分	7月23日 11:10 ~ 12:30	3	共壹頁

註：考生可否攜帶計算機或其他資料作答，請在備註欄註明（如未註明，一律不准攜帶）

**Part I. 填充題**（只需寫出答案即可，但請務必標明題號；每個空格 5 分，共 50 分。）

1. Find the domain of the function  $f(x) = \frac{1}{\sqrt{x-1}} + \frac{1}{x^2-4}$ ? \_\_\_\_\_ (1)
2. Let  $f(x) = x^2 - 1$  and  $g(x) = \sqrt{x} + 1$ , compute the composite function  $f \circ g$ . \_\_\_\_\_ (2)
3. Evaluate  $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{x} =$  \_\_\_\_\_ (3)
4. Find the derivative of  $f(x) = \frac{(1-x^5)(x^2+1)^3}{x-2}$ . \_\_\_\_\_ (4)
5. Determine the intervals where the function  $f(x) = x^3 - 3x^2 - 24x + 32$  is increasing. \_\_\_\_\_ (5)
6. Find the absolute maximum of  $f(x) = x - 2\sqrt{x}$  on the interval  $[0, 9]$ . \_\_\_\_\_ (6)
7. Use logarithmic differentiation to find the derivative of  $f(x) = x^x$  ( $x > 0$ ). \_\_\_\_\_ (7)
8. Evaluate  $\int (2x + \frac{3}{x} + \frac{4}{x^2}) dx =$  \_\_\_\_\_ (8)
9. Evaluate  $\int (e^{-3x} + \frac{\ln x}{2x}) dx =$  \_\_\_\_\_ (9)
10. Evaluate  $\int_0^4 x\sqrt{9+x^2} dx =$  \_\_\_\_\_ (10)

**Part II. 計算題**（請詳列計算過程，否則不予給分；每題 10 分，共 50 分。）

1. Find the derivative  $f'$  of  $f(x) = \sqrt{1-2x}$  by using the definition of the derivative.
2. What is the slope of the tangent line to the graph of  $f(x) = (x^2+1)(2x^3-3x^2+1)$  at the point  $(2, 25)$ ?  
How fast is the function  $f$  changing when  $x = 2$ ?
3. Given the equation  $x^3 + 3xy + y^3 = 4$ , find  $\frac{dy}{dx}$  by implicit differentiation.
4. Determine the intervals where the function  $f(x) = \frac{1}{x^2+1}$  is concave upward and where it is concave downward and find the inflection points of  $f$ .
5. Find the area of the region completely enclosed by  $f(x) = x^3 - 3x + 3$  and  $g(x) = x + 3$ .