

# 大葉大學九十學年度研究所碩士班招生考試試題紙

系所 組別	考試科目 (中文名稱)	考試日期	備 註
電機工程 丁組	控制系統	4 月 22 日 第 3 節	可以使用尺，一般掌上計算器及 一般工程用計算器。不用抄題。

1. Given  $\frac{dx}{dt} = \mathbf{A}x(t) + \mathbf{B}u(t)$ ,  $y(t) = \mathbf{C}x(t)$ .  $\mathbf{A} = \begin{bmatrix} 0 & 3 & 1 \\ 2 & 8 & 1 \\ -10 & -5 & 2 \end{bmatrix}$ ,  $\mathbf{B} = \begin{bmatrix} 10 \\ 0 \\ 0 \end{bmatrix}$ ,  $\mathbf{C} = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$  (10%)

Use **Routh-Hurwitz** Stability Criterion to determine the **stability** of the system.

2. Given  $\frac{dx}{dt} = \mathbf{A}x(t) + \mathbf{B}u(t)$ .  $\mathbf{A} = \begin{bmatrix} -3 & -3 & -1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$ ,  $\mathbf{B} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$

Design a **state-feedback gain K** such that  $u(t) = -\mathbf{K}x(t)$  so that the **eigenvalues** of the closed-loop system are **-2, -2, -2**. (10%)

- 3(a). Determine **Z-transform** of a sequence,  $f(k) = \exp(-k)$ ,  $k \geq 0$ , and its **region of convergence**. (8%)

- 3(b). Find the **inverse Z-transform** of  $F(z) = \frac{z(2z+1)}{(z-1)(z-2)(z-3)}$  (8%)

- 3©. Find the **initial and final values of f(k)** if its Z-transform is

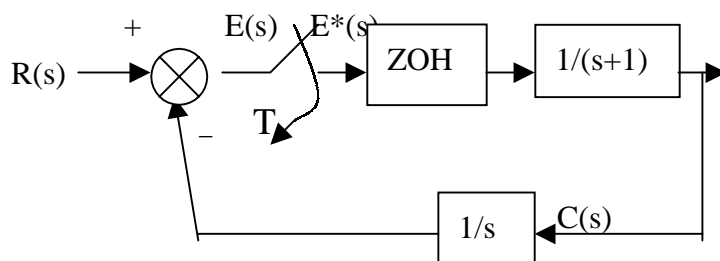
$$F(z) = \frac{0.792z^2}{(z-1)(z^2 - 0.416z + 0.208)}$$
 (8%)

4. Given the block diagram of a discrete-time control system as follows, where ZOH is Zero-Order-Hold with its transfer function of  $H_o(s) = (1 - \exp(-Ts))/s$ .  $T$  is the sampling period.

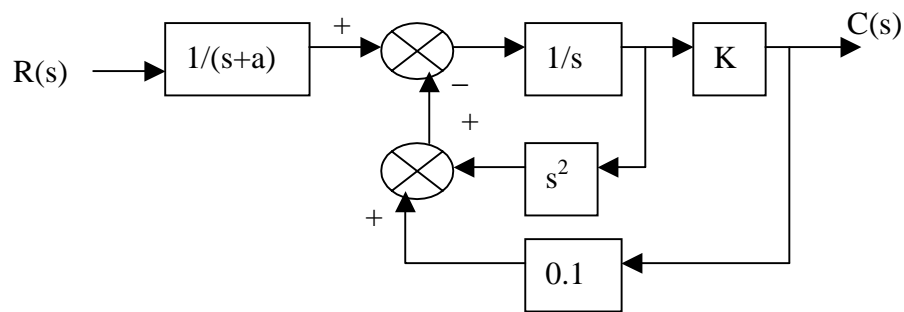
- (a). Find **C(s)/R(s)** when  $T_s = 1$  sec. (8%)

- (b). **Discuss its stability**. (8%)

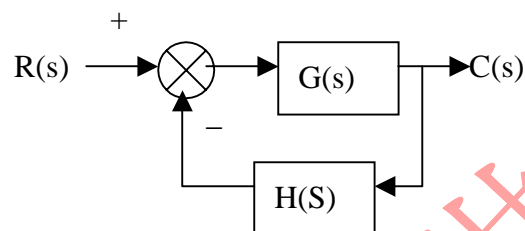
s-domain	z-domain
$1/s$	$1/(1-z^{-1})$
$1/(s+1)$	$1/(1-z^{-1}e^{-T})$
$1/s^2$	$Tz^{-1}/(1-z^{-1})^2$



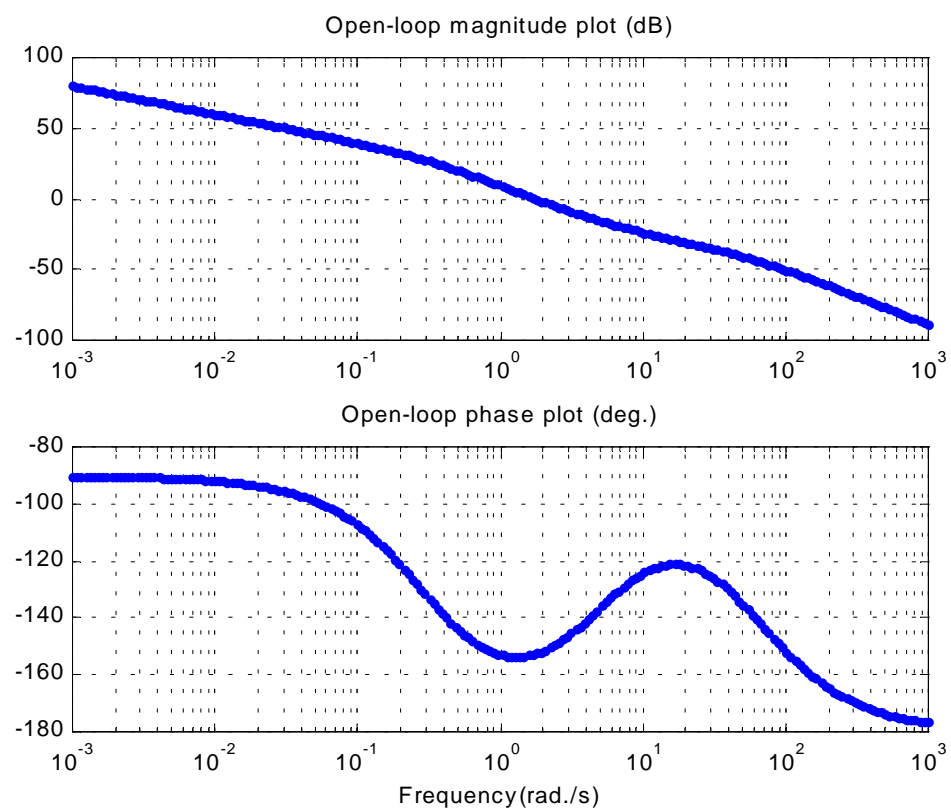
5. Use **Mason's signal flow** graph method to find  $C(s)/R(s)$ . (10%)



6. Given the block diagram and transfer functions:  $G(s)=10/[s(s+1)]$ ,  $H(s)=5$ , find **sensitivity  $S^{T(s)}_{G(s)}$  and  $S^{T(s)}_{H(s)}$**  respectively if  $T(s)$  is the closed-loop transfer function of the system when  $\omega=1$  rad/s. (10%)



7. Given **Bode diagram** of a specified continuous-time control system, **find its 3rd order Transfer function**. (10%)



8. A plant with its transfer function as  $G(s)=1/(s^2 + 3s +2)$ . If we want to use a continuous-time PID(Proportional-Integral-Derivative) controller with its transfer function  $D(s) = (s^2 + 6s + 15)/s$  in cascaded with  $G(s)$ , **draw its root locus clearly.** (10%)

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