

大葉大學九十學年度轉學招生考試試題紙

系 別	日\ 第二部	年級	考 試 科 目 (中 文 名 稱)	考試日期	節次	備註
資訊管理		二	微積分	七月 二十四日	三	

註：考生可否攜帶計算機或其他資料作答，請在備註欄註明（如未註明，一律准攜帶）
詳列計算步驟，否則一概不計分

10% 1. Evaluate (a) $\lim_{x \rightarrow 2} \frac{4(x^2 - 4)}{x - 2}$ (b) $\lim_{h \rightarrow 0} \frac{\sqrt{1+h} - 1}{h}$

15% 2. Find the values of x for which each of the following functions is continuous.

(a) $f(x) = 3x^3 + 2x^2 - x + 10$ (b) $g(x) = \frac{8x^{10} - 4x + 1}{x^2 + 1}$ (c) $h(x) = \frac{4x^3 - 3x^2 + 1}{x^2 - 3x + 2}$

20% 3. (a) Give the definition of the derivative $f'(x)$ of $f(x)$. (hint: The derivative of a function f

with respect to x is the function f' defined by $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}, \dots$)

(b) Let $f(x) = \frac{1}{x}$. Apply (a) to find $f'(x)$.

35% 4. Find the derivative of the following functions:

(a) $f(x) = x^{3.1}$ (b) $f(x) = \frac{x-1}{2x+1}$ (c) $f(x) = (x^3 + 1)^5$

(d) $f(x) = e^{2x^2+x}$ (e) $f(x) = x^x$

10% 5. Let $f(x) = 3x$.

(a) Sketch the region R under the graph of f on the interval $[0,2]$ and find its exact area using geometry.

(b) Use a Riemann sum with four subintervals of equal length ($n=4$) to approximate the area of R . Choose the representative points to be the left endpoints of the subintervals.

10% 6. Find the relative maxima and relative minima of the function $f(x) = x^3 - 3x^2 - 24x + 32$.